

Notes 4-3

Sec 1 H

More Vertical Shifts of Exponential Functions

Unit 4

Identify the y-intercept:

$$(0, a + k)$$

$$y = a \cdot b^x + k$$

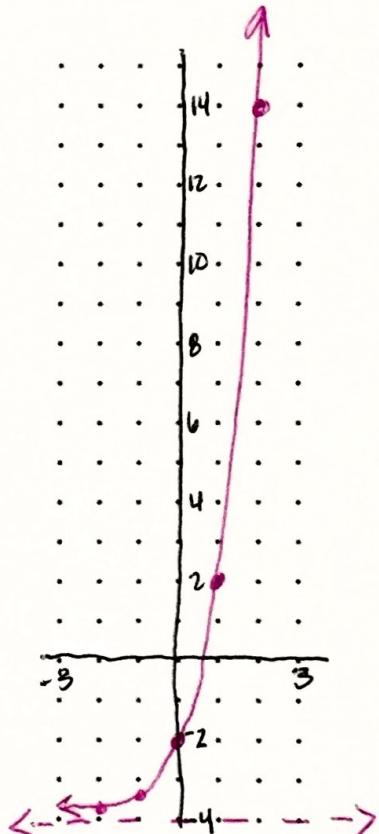
Identify the asymptote:

$$y = k$$

Graph.

Ex. 1: $f(x) = 2(3)^x - 4$

x	$2(3)^x$	$y - 4$
-2	$\frac{2}{9}$	-4 $\frac{-37}{9}$
-1	$\frac{2}{3}$	-4 $\frac{-31}{3}$
0	2	-2
1	6	2
2	18	14



What is the y-intercept? $(0, 2 + -4) = (0, -2)$

Where is the asymptote? $y = -4$

Are the functions increasing or decreasing?

Are the functions above or below their asymptotes?

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Graph.

Ex. 2: $f(x) = -5(2)^x + 6$

x	$-5(2)^x$	$y + 6$
-2	$-\frac{5}{4}$	$4\frac{3}{4}$
-1	$-\frac{5}{2}$	$3\frac{1}{2}$
0	-5	1
1	-10	-4
2	-20	-14

What is the y -intercept? $(0, -5+6)$

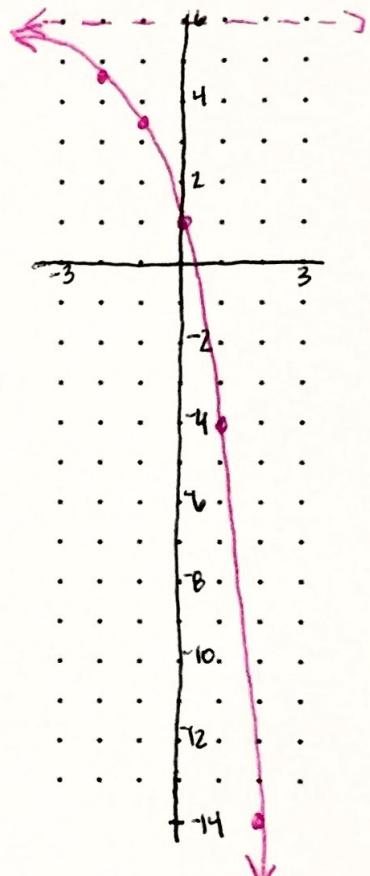
$$(0, 1)$$

Where is the asymptote?

$$y = 6$$

Are the functions increasing or decreasing?

Are the functions above or below the asymptotes?



Ex. 3: $f(x) = -3\left(\frac{1}{2}\right)^x + 5$

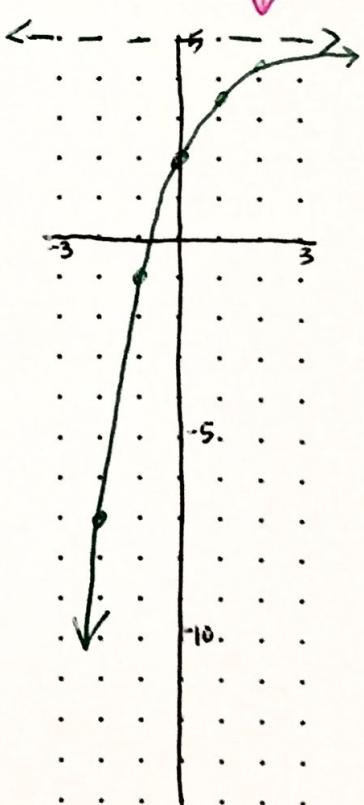
x	$-3\left(\frac{1}{2}\right)^x$	$y + 5$
-2	-12	-7
-1	-6	-1
0	-3	2
1	$-\frac{3}{2}$	$3\frac{1}{2}$
2	$-\frac{3}{4}$	$4\frac{1}{4}$

What is the y -intercept? $(0, 2)$

Where is the asymptote? $y = 5$

Are the functions increasing or decreasing?

Are the functions above or below the asymptotes?



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Example 4:

For this problem you are given the parent function $f(x) = -2(3)^x$ and a second function $g(x) = -2(3)^x + 4$ that has been shifted vertically.

- Create a table for both $f(x)$ and $g(x)$.
- Graph both $f(x)$ and $g(x)$ on the same graph. Use graph paper. Make sure to label your axis and draw the asymptotes.
- Answer the following questions.

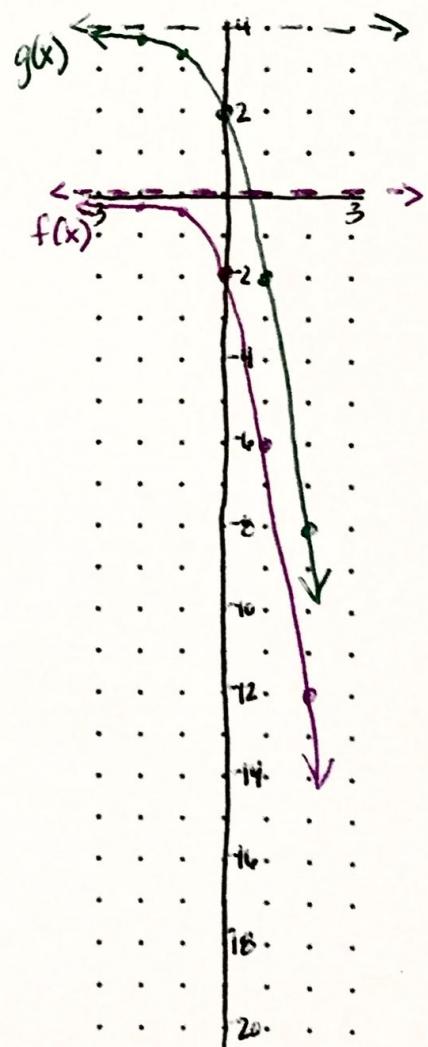
What is the y -intercept? $f(x) : \underline{(0, -2)}$ $g(x) : \underline{(0, 2)}$

Where is the asymptote? $f(x) : \underline{y=0}$ $g(x) : \underline{y=4}$

Are the functions increasing or decreasing?

Are the functions above or below their asymptotes?

x	$f(x) = -2(3)^x$	$g(x) = -2(3)^x + 4$
-2	$-\frac{2}{9}$	$3\frac{7}{9}$
-1	$-\frac{2}{3}$	$3\frac{1}{3}$
0	-2	2
1	-6	-2
2	-12	-8



Identify the y -intercept and the asymptote for each function.

Ex. 5: $f(x) = 4(2)^x - 1$

$y\text{-int: } (0, 4-1) \rightarrow (0, 3)$

asym: $y = -1$

Ex. 6: $g(x) = -5(2)^x$

$y\text{-int: } (0, -5)$

asym: $y = 0$

Ex. 7: $h(x) = 5^x - 7$

$y\text{-int: } (0, 1-7) \rightarrow (0, -6)$

asym: $y = -7$

Ex. 8: $f(x) = \frac{1}{4}(3)^x + 1$

$y\text{-int: } (0, \frac{1}{4}+1) \rightarrow (0, 1\frac{1}{4})$

asym: $y = 1$

Ex. 9: $f(x) = -9(2)^x + 17$

$y\text{-int: } (0, 8)$

asym: $y = 17$